

## PLASMONIC AG-LINBO<sub>3</sub> METAMATERIAL: A STUDY OF DIELECTRIC AND OPTICAL PROPERTIES

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### Abstract

We report the optical and dielectric properties of a multilayer system constituted by ITO, an square-arrangement of Ag nanoparticles (NPs) on the uniaxial LiNbO<sub>3</sub>, the polymer PMMA and the substrate SiO<sub>2</sub>. We investigate the compositional and geometrical parameters dependences on the optical absorption of the stacked layers. The effective dielectric function of the ensemble aggregates of Ag NPs and uniaxial LiNbO<sub>3</sub> crystal is treated through the extended Maxwell-Garnett approximation. The multilayer absorbance is determined by means of the Transfer Matrix Method. We demonstrate that an adequate choice of structural parameters such as NPs sizes, interparticle distances and layers thicknesses can produce an enhancement of optical absorption in the multilayer. In addition, we evaluate the dielectric modulus parameter of the effective medium layer in the perpendicular and parallel directions of the Ag NPs plane. For both directions, when the filling factor is big enough, we find the negative epsilon (NE) condition, typical characteristic observed in metamaterials.

**Keywords:** Optical properties, Dielectric properties, Multilayer with Ag NPs on LiNbO<sub>3</sub>; Negative epsilon condition

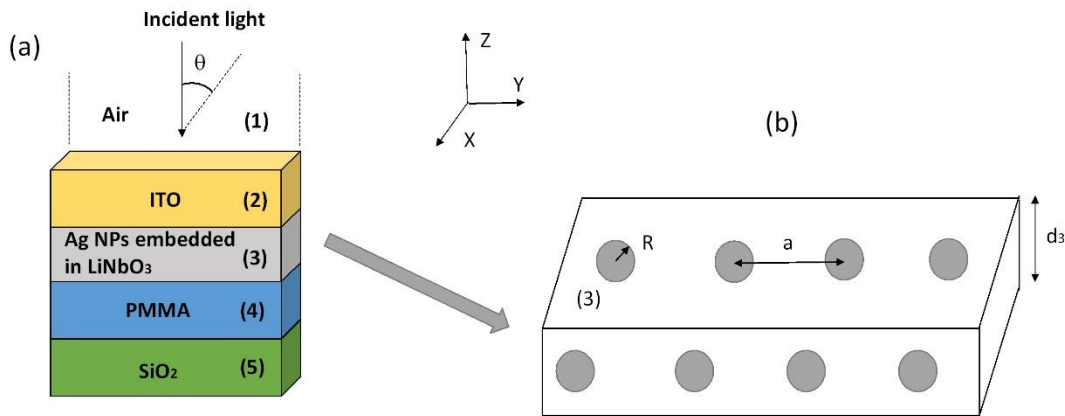
### 1. INTRODUCTION

Noble metal nanostructures exhibit the capability to couple light with the collective oscillations of their conduction-band electrons, known as surface plasmon resonance (SPR), which can result into a strong confinement of the electromagnetic field in the vicinity of the metallic physical boundaries. This characteristic can be used in many applications such as light-emitting systems, biosensors or solar cells [1]. Sun et al. [2] reported the photodetector ability of LiNbO<sub>3</sub> on insulator with encapsulated plasmonic nanoparticles and doped silver ions. On the other hand, we previously investigated the anisotropy dielectric tensor of the rectangular arrangement of Ag nanoparticles (NPs) on LiNbO<sub>3</sub> matrix as a composite system [3]. From the array's effective dielectric function, we studied the compositional and geometrical parameters which could satisfy the negative epsilon (NE) condition, typical in metamaterials, but we did not investigate their optical absorbance nor their dielectric properties.

Therefore, in the present paper, the optical absorption of a multilayer with a square array of Ag NPs on LiNbO<sub>3</sub> matrix is evaluated by using an extended Maxwell-Garnett (M-G) theory [4] and the Transfer Matrix Method (TMM) [5]. We study the compositional and geometrical parameters which influence the optical absorption of the multilayer. In addition, from the dielectric modulus parameter, we investigate the NE condition and the involved resonances for the Ag NPs arrangement in LiNbO<sub>3</sub> crystal in the perpendicular and parallel directions to the Ag NPs plane.

## 2. INVESTIGATED SYSTEM AND THEORETICAL MODEL

**Figure 1** depicts the scheme of the multilayer constituted by (1) a semi-infinite air space; (2) a layer of ITO, transparent in the VIS range, with dielectric function  $\varepsilon_2$  and thickness  $d_2$ ; (3) the effective medium composed by a square arrangement of Ag NPs embedded in  $\text{LiNbO}_3$ , with thickness  $d_3$  and dielectric function described later; the layer (4) of transparent thermoplastic PMMA, with dielectric function  $\varepsilon_4$  and thickness  $d_4$ ; and (5) the substrate of  $\text{SiO}_2$  with dielectric function  $\varepsilon_5$  and fixed thickness  $d_5 = 2000$  nm. The light impinges from the air with dielectric function  $\varepsilon_1 = 1$ .



**Figure 1** Scheme of the investigated multilayer (figure 1a). Figure 1b is the zoom of the effective medium layer

The dielectric function of ITO is described by Drude model [6], while the refractive indexes of PMMA,  $\text{SiO}_2$  and  $\text{LiNbO}_3$  are taken from reference [7]. The Ag NPs are located at  $xy$  plane (square lattice) and they are separated by interparticle distances ( $a$ ). The array is characterized by spheres with radii  $R$  and the interparticle distance ( $a$ ) is chosen such that  $R/a = 0.25$ . Due to the 2D arrangement of Ag NPs, and accounting on interparticle interaction in dipolar approximation; the sum of dipolar electric fields does not cancel out [4]. Accordingly, one expects dissimilar contributions to the local electric field when the electric field is applied perpendicular or parallel to the NPs in-plane. That dissimilar responses results in an anisotropic dielectric function for the layer 3. Following the same treatment than in ref. [3], we deduce for square lattice the corresponding effective dielectric functions:  $\varepsilon_3^\perp(\omega)$  and  $\varepsilon_3^\parallel(\omega)$ , extensively described in ref. [3].

With the knowledge of the dielectric permittivity of each layer, we use the TMM for our system, similar to that reported in ref. [8]. Using the expressions for the reflectance,  $R$ , and transmittance,  $T$ , one calculate the absorbance ( $A$ ) of light in such stacked layers by means of the standard relation:  $A = 1 - R - T$ .

Focusing on the dielectric properties of the effective medium layer in the perpendicular and parallel directions, we evaluate the real and imaginary parts of the dielectric modulus,  $M$ , defined in ref. [9].

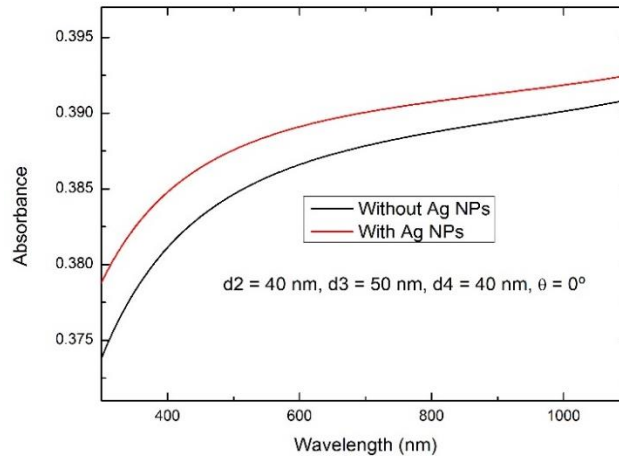
## 3. RESULTS AND DISCUSSION

To clarify the presentation of our results, we subdivide the discussion in the following two subsections.

### 3.1 Optical absorbance of the multilayer system

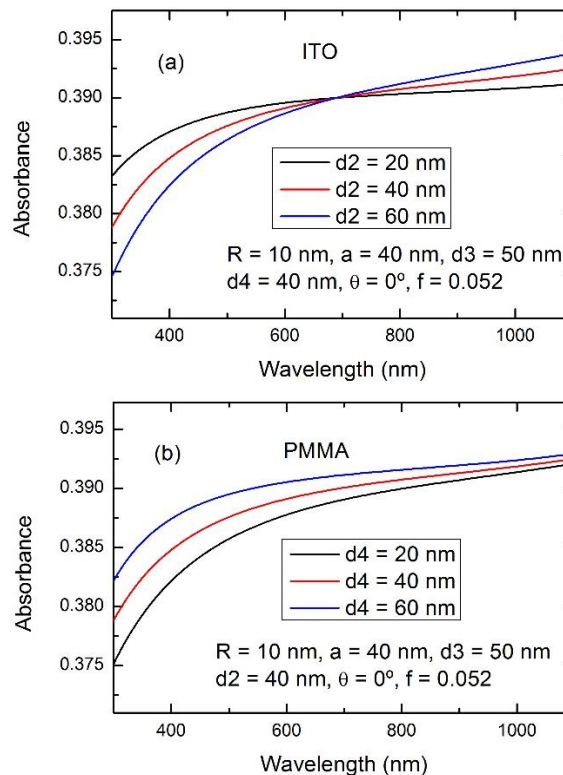
In order to know the influence of the Ag NPs in the absorbance of the investigated system, we show in **Figure 1** the multilayer absorbance with and without Ag NPs at normal incidence with  $\lambda = 450$  nm. The presence of Ag NPs benefit the excitation of plasmonic modes, which entails an absorption enhancement of 25%. He et al.

[10] proved both experimentally and theoretically the Ag NPs induced surface plasmonic modes centered at 459 nm. On the other hand, Sun et al. [2] showed an enhancement of the absorption in the VIS range with the inclusion of Ag NPs in LiNbO<sub>3</sub> crystal. For both cases, with and without Ag NPs, the absorbance values increase for greater wavelength until a saturation value around 0.4 at 1100 nm.



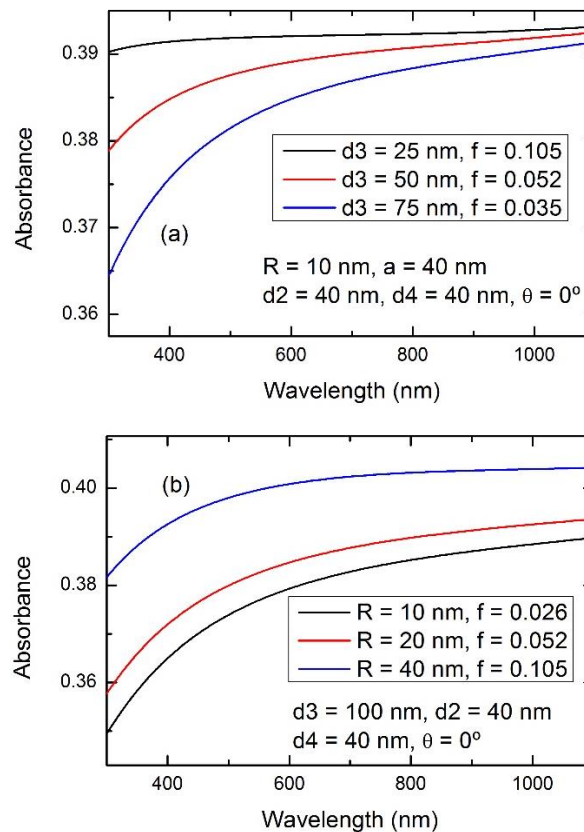
**Figure 2** Absorbance of the stacked layers with and without Ag NPs arrangement in the layer 3.

In order to investigate the thicknesses effect on the stacked layers absorbance, we evaluate their dependences modifying the thicknesses of ITO, PMMA and the effective medium layers. **Figure 3a** depicts the stacked layers absorbance for different ITO thicknesses ( $d_2 = 20$  nm, 40 nm and 60 nm), fixing  $d_3 = 50$  nm and  $d_4 = 40$  nm. For higher ITO thickness, we obtain a greater absorbance for  $\lambda > 600$  nm, while for shorter  $\lambda$ , the greater absorbance relates to the smallest ITO thickness. We identified  $\lambda = 700$  nm, where the three absorption spectra have a crossing point. We show in **Figure 3b** the absorbance dependence on the PMMA thickness



**Figure 3** Absorbance of the multilayer for different thicknesses of ITO layer,  $d_2$  (a) and PMMA layer,  $d_4$  (b).

( $d_4 = 20$  nm, 40 nm and 60 nm), fixing  $d_2 = 40$  nm and  $d_3 = 50$  nm. On the contrary to the dependence of the ITO thickness, we obtain greater absorbance values for PMMA thicker layers in all wavelength range. Although it is not shown here, for greater thickness of PMMA layer ( $d_4 = 100$  nm, 200 nm, 400 nm), the behavior of absorbance with the thickness is analogous to the case of ITO; i.e., there are crossing points in the optical spectra. Attending to the effective medium thickness dependence, **Figure 4a** shows the absorbance for  $d_3 = 25$  nm, 50 nm and 75 nm with fixed  $R = 10$  nm,  $a = 40$  nm,  $d_2 = 40$  nm and  $d_4 = 40$  nm. A different  $d_3$  thickness imply a different filling factor,  $f$ . For higher  $f$ , the absorbance values increase and then, a greater concentration of Ag NPs entails a greater optical absorption of the multilayer. We observe a saturation value around 0.4 for  $\lambda > 800$  nm. In addition, we investigate the Ag NPs geometrical parameter size effects on the multilayer absorbance. **Figure 4b** depicts the absorbance for radii  $R = 10$  nm, 20 nm and 40 nm, where  $R/a = 0.25$ , fixing  $d_3 = 100$  nm,  $d_2 = 40$  nm and  $d_4 = 40$  nm. We obtain greater absorbance values for higher NPs density ( $f = 0.105$ ). We previously discussed that higher concentration of Ag NPs benefit the absorption of the multilayer. The effective medium (layer 3) constitutes the active layer in this stacked system.



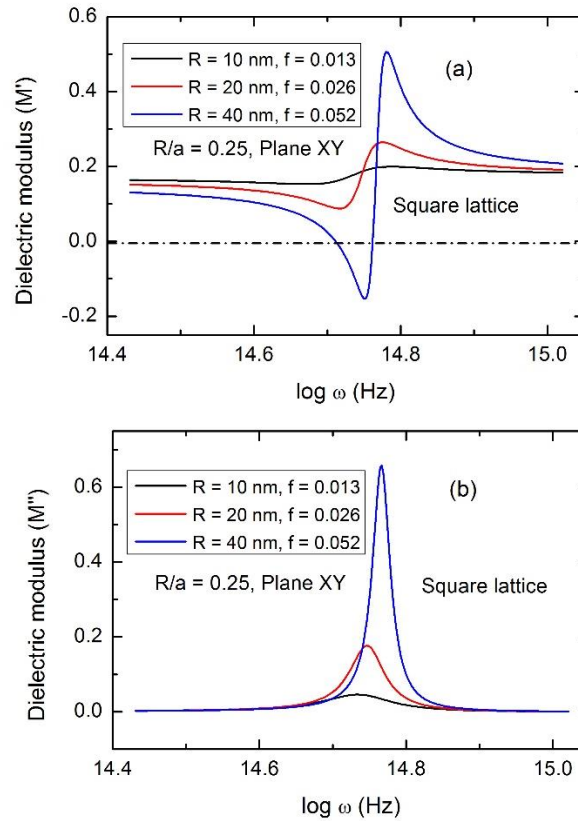
**Figure 4** Absorbance of the multilayer for different thickness of effective medium layer,  $d_3$  (a) and for different radii and interparticle distance of Ag NPs lattice (b), which implies different filling factor,  $f$ .

In summary, we identify a direct relationship between absorbance intensity and filling factor values.

### 3.2 Dielectric properties of the active layer

Attending to the dielectric properties of the effective medium layer, we show in **Figure 5** the dielectric modulus (real and imaginary parts) in the parallel direction of Ag NPs plane ( $xy$  plane) with different filling factors. For both real and imaginary parts, we observe a resonance around  $5.6 \times 10^{14}$  Hz, which is blue shifted for increasing  $f$ . For  $f = 0.052$ ,  $M'$  becomes negative in a frequency interval centered at  $5.6 \times 10^{14}$  Hz; then, the NE condition ( $\epsilon_{\text{eff}}' < 0$ ) is obtained for specific values of radii or filling factor. This feature was previously

reported in refs. [3,9]. This kind of negative dielectric behavior is observed in metamaterials due to the plasmonic resonance as suggested by Drude model [11]. For NE condition, the displacement of carriers is opposite to the direction of electric field,  $\mathbf{E}$ . Consequently, the  $\mathbf{D}$  vector is aligned opposite to  $\mathbf{E}$ . In fact, this produces the negative polarization leading to the negative epsilon or dielectric constant value.



**Figure 5** Real- (a) and imaginary- (b) parts of the dielectric modulus dependences on  $\log \omega$  in the xy plane direction. The horizontal dashed line in fig 5a remarks the NE condition.

Although it is not shown here, we obtain a resonance around  $7.9 \times 10^{14}$  Hz for the dielectric modulus (real and imaginary parts) in the perpendicular direction of the Ag NPs plane (z axis). For  $f = 0.052$ , the NE condition is reached in a frequency interval centered at  $7.9 \times 10^{14}$  Hz.

In summary, the NE condition, typical in metamaterials, is obtained in the ordinary as well as in extraordinary directions of the Ag NPs plane for filling factor big enough ( $f = 0.052$ ).

#### 4. CONCLUSION

We have evaluated the optical absorption of a multilayer system composed by ITO, a square-lattice of Ag NPs in uniaxial  $\text{LiNbO}_3$  crystal, PMMA and a substrate of  $\text{SiO}_2$ . We investigated the geometrical parameters dependences on the multilayer optical absorption. The stacked layers absorption is simulated by TMM using an extended M-G model to define the dielectric function of the effective medium. We observed that an adequate choice of geometrical parameters such as NPs sizes and layers thicknesses can produces an enhancement of optical absorption of the multilayer. Indeed, when the filling factor is higher, the multilayer absorbance is greater. In addition, we evaluated the dielectric modulus parameter of the effective medium layer (active layer) in the parallel and perpendicular directions of the Ag NPs plane. For both directions, when  $f = 0.052$ , we found the NE condition, typical feature observed in metamaterials.

## ACKNOWLEDGEMENTS

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